

RePRINTED 5-9-19  
CORRECTED PHONE #

# HEIGHTS TOWER SYSTEMS

Manufacturers of Aluminum Towers and Structures

## ORDER ACKNOWLEDGEMENT

Date: 4/29/2019  
QUOTE # 19-429

To: Steve Koogler  
8865 Barrington Way  
Springboro, OH 45066  
Email: [k8dzsteve@gmail.com](mailto:k8dzsteve@gmail.com)  
→ Ph#: 937-266-5507

Ship To: Steve Koogler  
8865 Barrington Way  
Springboro, OH 45066

For a 64 ft. aluminum stacked tower rated for 22 sq. ft. in winds of 80 mph, mounted on a Fold Over Kit. Overall height of tower on Stand is approx. 69 ft., not incl. mast, which will add more height.

Supervisor	Est. Ship Time	FOB	SHIP VIA
DD	12+ Weeks ARO	Pensacola, FL	Van Truck
LINE	QTY	PRODUCT I.D.	DESCRIPTION
1	1	A64 22sq@80mph, consist	A64 22sq ft@80 mph, consisting of 8 ft. sections:
2	2	AC18-131	Aluminum Center Section - 8 ft. length
3	1	AC18-172	Aluminum Center Section - 8 ft. length
4	1	AJ22-172	Aluminum Junction Section - 8 ft. length
5	1	AC22-225	Aluminum Center Section - 8 ft. length
6	1	AJ26-225	Aluminum Junction Section - 8 ft. length
7	1	AJ30-225	Aluminum Junction Section - 8 ft. length
8	1	AC30-288	Aluminum Center Section - 8 ft. length
9	1	HBT30-288	Hinge Base, 30-288, threaded adjustable version
10	1	Rebar Cage	Pre-fabricated Rebar Cage for base pad
11	1	4' Stand, 30-288	Four Foot Stand, 30-288, for Fold Over Kit
12	1	FOK30-288	Fold Over Kit, 30-288, all aluminum
13	1	Screw System, 1.25"	Screw Actuator System, 1.25" dia, for Fold Over Kit
14	1	Pre-Wired GM Kit	Pre-wired Gearmotor Kit, for FOK, OPTIONAL
15	1	TS18-131	Top Shelf 18-131, drilled for GS-065
16	1	GS-065	Yaesu Thrust Bearing, GS-065, up to 2.66" OD mast capacit
17	1	RS18-131	Rotor Shelf 18-131, drilled for rotor
18	1	Grdg Kit, 3 leg	Grounding Kit, lightning protection, 3 ground rods, cable,etc
19	1	Cals/Diagram	Non-Stamped Calcs and Diagrams per the 2009 IBC
20	1	Packaging	Palletting and Packaging
21	1	Est. Shipping	Estimated Shipping to OH -- Price subject to change

Thank you for the opportunity to quote your tower project.

Please let us know if you have any questions.

TOWER PROFILE

<CUA66 18stf@ 70 mph w FOK B.xls><CUA88 20stf@ 70 mph w FOK.xls><A64 22stf@80mph w FOK.xls>

MAXIMUM ANTENNA WINDLOAD OF 22 SQ. FT.  
AT 1' - ABOVE TOP IN 80 MPH WINDS EN  
TOWER (69') PER 2009 INTL. BLDG. CODE.

HEIGHTS TOWER SYSTEMS

1529 Gulf Beach Hwy.  
Pensacola, FL 32507  
(850) 455-1210  
(850) 455-4355 FAX

Model: A64 22stf@80mph on FDK  
64 Ft. Tapered Fold Over Tower  
mounted on 4 Ft. Stand. Overall  
height on Stand is 69 Ft.

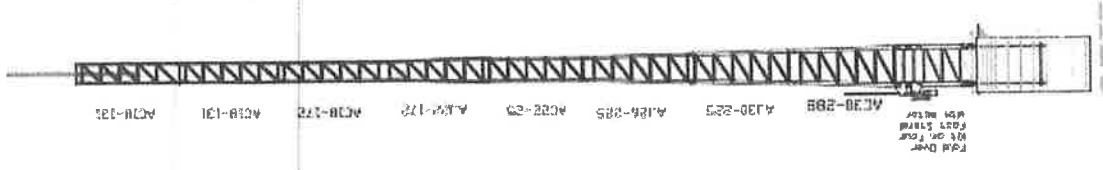
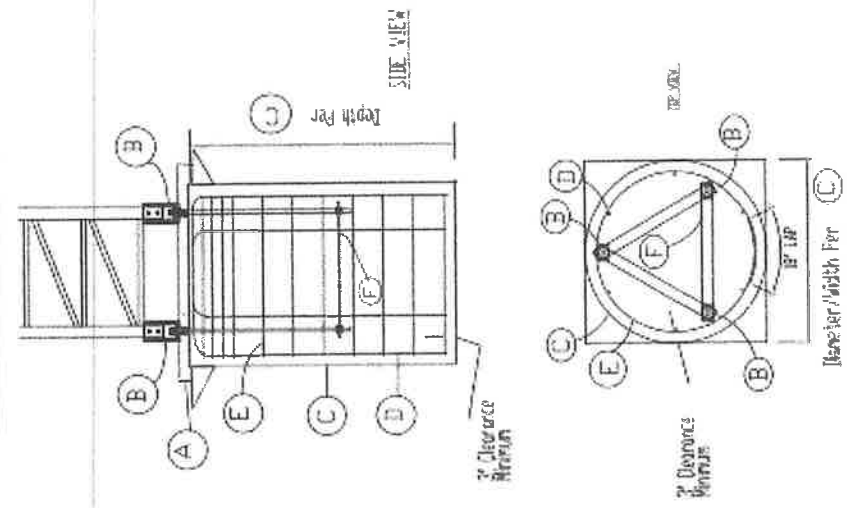
Customer: Steve Koogler  
Springboro, OH 45066  
Date: May 9, 2019

Drawing NOT TO SCALE

FOUNDATION NOTES:

- (A) FOUNDATION SHOULD BE AT LEAST 1' TO 3" ABOVE GRADE
- (B) TOWER BASE CLEVIS ASSY. BELTED TO 125' & THREADED RODS, BT ALLOW TO BE EMBEDDED A MINIMUM 54" DEPTH
- (C) CONC FTG - 5' DIAMETER AND 7" BELOW GRADE IF CIRCULAR DEPTH MAY BE REDUCE IF SAME FOUNDATION USED
- (D) 160 DR. 60 VERT BARS W/STD HOOK @ TOP - 3/4" SIZE PER CALCULATION, BE SIZE
- (E) 48 #3 BARS @ 4" @ TOP OF FTG, 160 BARS @ 12" @ ELSEWHERE PER CALCULATION
- (F) FLATBAR SPACER BARS, 3" x 1/4", DRILLED ON TOWER LEG CENTERS OF 285", 125" HOLES, AS SPECIFIED IN CALCULATIONS

TOWER FOUNDATION



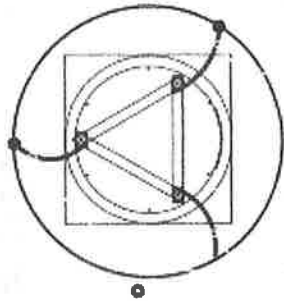
TOWER NOTES: UNLESS OTHERWISE SPECIFIED

1. THE TOWER SHALL BE FABRICATED AND ASSEMBLED IN ACCORDANCE WITH THE 2009 INTERNATIONAL BLDG. CODE.
2. CONCRETE SLUMP SHALL NOT EXCEED 4-1/2 INCHES AND CONCRETE SHALL MEET A MINIMUM COMPRESSIVE STRENGTH OF 2500 PSI AT 28 DAYS.
3. THE FOUNDATION DESIGN IS ADEQUATE FOR SITES WITH ALLOWABLE LATERAL BEARING VALUES GREATER THAN OR EQUAL TO 150 LBS./SQ. FT./FSIOT AT DEPTH AS LISTED IN THE 30C.
4. FOUNDATION WIDTH MAY BE SIZED FROM 5' TO 6' WITHOUT ADVERSE IMPACT ON FOUNDATION BASE AND MAY HAVE EITHER AN IRREGULAR SHAPE OR BE RECTANGULAR. SHALL BE CENTERED ACCORDINGLY AND REQUIRRED CONCRETE WILL VARY BETWEEN APPROX. 55 TO 8 CUBIC YARDS, DEPENDING ON EXACT SHAPE. ORDER ENGINE READY-MIX LOAD TO AVOID SHORTAGE.

SECTION SIZES (Inches)

SIZE	Leg	Di.	Leg	Vol.	Letter	Di.
10-18	12"	144"	172"	976'		172"
10-12	12"	144"	172"	976'		172"
22-22	22"	225"	225"	120	508'	225"
26-22	26"	225"	225"	120	508'	225"
34-22	34"	225"	225"	120	508'	225"
34-28	34"	288"	288"	1276	1546'	288"
34-STAIR	28"	327"	327"	131'	514'	327"

Material: 6061 T6 Alum. for legs, 6061 T6 for lattice rods





# HEIGHTS TOWER SYSTEMS

1529 Gulf Beach Hwy • Pensacola, FL 32507  
Phone (850) 455-1210 • Fax (850) 455-4355  
www.heightstowers.com

## CALCULATIONS - Steve Koogler

### 64-FOOT TAPERED ALUMINUM TOWER—80MPH WIND SPEED (OVERALL HEIGHT ON STAND IS 69-FOOT)

#### PROJECT DATA

Tower Height:	$h_{tot} := 69\text{-ft}$		
Antenna Wind Area:	$A_{ant} := 21\text{-ft}^2$	Rotor Wind Area:	$A_{rot} := 1\text{-ft}^2$
Antenna Weight:	$W_{ant} := 150\text{-lbf}$	Rotator Weight:	$W_{rot} := 35\text{-lbf}$
Basic Wind Speed:	$bws := 80\text{-mph}$		

#### DESIGN CRITERIA

##### BUILDING CODE

##### 2009 International Building Code

##### WIND LOAD IBC 2009 Sec.1609

Wind Velocity Pressure: ASCE 7-10 Ch. 27	$BWS := (85\ 90\ 100\ 105\ 110\ 120\ 125\ 130\ 140\ 150\ 160\ 170)^T \cdot \text{mph}$
$Q_s = 0.00256 \cdot V^2$	$Q_s := (18.5\ 20.7\ 25.6\ 28.2\ 31.0\ 36.9\ 40.0\ 43.3\ 50.2\ 57.6\ 65.5\ 74.0)^T \cdot \text{psf}$
	$q_s(bws) := \max(\text{linterp}(BWS, Q_s, bws), Q_{s0})$

Topographic Factor: ASCE 7-10 Section 26.8.2	$K_{zt} := 1.0$
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Wind Directionality Factor: ASCE 7-10 Section 26.6	$K_d := 0.85$
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Gust Factor: ASCE 7-10 Section 26.9	$G_{\text{wv}} := 0.85$
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Velocity Pressure Coefficients: ASCE 7-10 Table 27.3-1, Exposure "D"	$H_{\text{wv}} := (15\ 20\ 25\ 30\ 40\ 50\ 60\ 70\ 80)^T \cdot \text{ft}$
	$K_z := (1.03\ 1.08\ 1.12\ 1.16\ 1.22\ 1.27\ 1.31\ 1.34\ 1.38)^T$

Force Pressure Coefficient: ASCE 7-10 Figure 29.5-1 & 29.5-2	$K_z(h) := \max(\text{linterp}(H, K_z, h), K_{z0})$	$C_f := 1.3$ Cylindrical elements, < 2" in diameter.	$C_{fAnt} := 1.3$	$C_{fRot} := 1.3$
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Design Wind Load Functions: ASCE 7-10 Section 29.5	$P_w(h, bws) := 0.6(K_z(h) \cdot q_s(bws) \cdot K_d \cdot K_{zt}) \cdot C_f \cdot G$	Tower
	$P_{wAnt}(h, bws) := 0.6(K_z(h) \cdot q_s(bws) \cdot K_d \cdot K_{zt}) \cdot C_{fAnt} \cdot G$	Antenna
	$P_{wRot}(h, bws) := 0.6(K_z(h) \cdot q_s(bws) \cdot K_d \cdot K_{zt}) \cdot C_{fRot} \cdot G$	Rotator

### TOWER SECTION PROPERTIES

Section Index Values:  $i =$  0 1 2 3 4 5 6  
 11" 14" 18" 22" 26" 30" 35"

Leg Tube Index Values:  $j =$  0 1 2 3 4  
 100 131 172 225 288

Tower Section Length:  $L_s := 8 \cdot \text{ft}$

Tower Section Leg Moment Arm:  $d := (8.66 \ 11.26 \ 14.51 \ 17.75 \ 21.22 \ 24.68 \ 28.80)^T \cdot \text{in}$

Tower Section Allowable Moment:  $M_R :=$

	100	131	172	225	288	350	400	288S	
	4200	6900	0	0	0	0	0	0	0
	5400	8900	17300	0	0	0	0	0	0
	0	11400	22100	38500	0	0	0	0	0
	0	30000	26900	47200	0	0	0	0	0
	0	0	32000	56400	85400	0	0	0	0
	0	0	37200	65600	96300	135400	0	0	0
	0	0	43100	76500	112300	158000	0	333100	0
	0	0	0	0	0	185300	0	389400	0
	0	0	0	0	0	223400	200500	453300	0
					288	350	400	288S	

· lbf · ft

Tower Section Allowable Shear:  $V_R :=$

	390	390	0	0	0	0	0	0	0
	740	750	770	0	0	0	0	0	0
	0	1210	1230	1270	0	0	0	0	0
	0	1760	1820	1820	0	0	0	0	0
	0	0	2290	2350	2560	0	0	0	0
	0	0	1930	1990	2050	4580	0	0	0
	0	0	2320	2380	2450	3580	0	3470	0
	0	0	0	0	0	2230	0	3290	0
	0	0	0	0	0	2230	3050	2940	0

· lbf

Tower Section Wind Areas:  $A_w :=$

	1.8	2.2	0	0	0	0	0	0	0
	1.9	2.3	2.9	0	0	0	0	0	0
	0	2.5	3.0	3.7	0	0	0	0	0
	0	0	3.3	4.0	0	0	0	0	0
	0	0	3.5	4.2	5.0	0	0	0	0
	0	0	3.7	4.4	5.2	6.24	0	0	0
	0	0	4.1	4.8	5.6	6.5	0	5.70	0
	0	0	0	0	0	9.92	0	8.62	0
	0	0	0	0	0	9.92	11.11	8.94	0

· ft<sup>2</sup>

Tower  
Section  
Weight:

$$W_s := \begin{pmatrix} 15 & 20 & 0 & 0 & 0 & 0 & 0 & 0 \\ 19 & 23 & 36 & 0 & 0 & 0 & 0 & 0 \\ 0 & 28 & 40 & 59 & 0 & 0 & 0 & 0 \\ 0 & 0 & 46 & 65 & 0 & 0 & 0 & 0 \\ 0 & 0 & 54 & 73 & 93 & 0 & 0 & 0 \\ 0 & 0 & 58 & 77 & 96 & 131 & 0 & 0 \\ 0 & 0 & 70 & 89 & 108 & 138 & 0 & 243 \\ 0 & 0 & 0 & 0 & 0 & 218 & 0 & 372 \\ 0 & 0 & 0 & 0 & 361 & 217 & 217 & 388 \end{pmatrix} \cdot \text{lbf}$$

## TOWER DESIGN

### TOP OF TOWER (Antenna / Rotator)

Top of Tower:  $h := h_{\text{top}}$

Shear @ Top of Tower:  $V := P_{w\text{Ant}}(h, \text{bws}) \cdot A_{\text{ant}} + P_{w\text{Rot}}(h, \text{bws}) \cdot A_{\text{rot}} \quad V = 306.7 \cdot \text{lbf}$

Weight @ Top of Tower:  $W := W_{\text{ant}} + W_{\text{rot}} \quad W = 185 \cdot \text{lbf}$

Moment @ Top of Tower:  $M := 0 \cdot \text{lbf} \cdot \text{ft}$

Tower Section Length:  $L_s := 12 \cdot \text{ft}$

### SECTION 1

Tower Section Length:  $L_s := 8 \cdot \text{ft}$

Section Size Index:  $i := 2$       Leg Tube Index:  $j := 1$

Wind Area:  $A_{w_{i,j}} = 2.5 \text{ ft}^2$       Allowable Moment:  $M_{R_{i,j}} = 11400 \cdot \text{lbf} \cdot \text{ft}$

Weight:  $W_{s_{i,j}} = 28 \cdot \text{lbf}$       Allowable Shear:  $V_{R_{i,j}} = 1210 \cdot \text{lbf}$

Bottom Height:  $h_j := h - L_s \quad h = 61 \text{ ft}$

Wind Force on Section:  $F_{\text{wind}} := P_w \left( h + \frac{L_s}{2}, \text{bws} \right) \cdot A_{w_{i,j}} \quad F_{\text{wind}} = 34.5 \cdot \text{lbf}$

Weight @ Bottom:  $W := W + W_{s_{i,j}} \quad W = 213 \cdot \text{lbf}$

Moment @ Bottom:  $M := M + V \cdot L_s + F_{\text{wind}} \cdot \frac{L_s}{2} + \frac{W}{3} \cdot d_i \quad M = 2677 \cdot \text{lbf} \cdot \text{ft} < M_r \rightarrow \text{OK}$

Shear @ Bottom:  $V := V + F_{\text{wind}} \quad V = 341 \cdot \text{lbf} < V_r \rightarrow \text{OK}$

REQUIRED SECTION: **18" x 131**

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## SECTION 2

Tower Section Length:

$$L_s := 8 \cdot \text{ft}$$

Section Size Index:

$$i := 2$$

Leg Tube Index:

$$j := 1$$

Wind Area:

$$A_{w_{i,j}} = 2.5 \text{ ft}^2$$

Allowable Moment:

$$M_{R_{i,j}} = 11400 \cdot \text{lb} \cdot \text{ft}$$

Weight:

$$W_{s_{i,j}} = 28 \cdot \text{lb} \cdot \text{ft}$$

Allowable Shear:

$$V_{R_{i,j}} = 1210 \cdot \text{lb} \cdot \text{ft}$$

Bottom Height

$$h := h - L_s$$

$$h = 53 \text{ ft}$$

Wind Force on Section:

$$F_{wind} := P_w \left( h + \frac{L_s}{2}, bws \right) \cdot A_{w_{i,j}}$$

$$F_{wind} = 33.8 \cdot \text{lb} \cdot \text{ft}$$

Weight @ Bottom:

$$W := W + W_{s_{i,j}}$$

$$W = 241 \cdot \text{lb} \cdot \text{ft}$$

Moment @ Bottom:

$$M := M + V \cdot L_s + F_{wind} \cdot \frac{L_s}{2} + \frac{W}{3} \cdot d_i$$

$$M = 5639 \cdot \text{lb} \cdot \text{ft} < M_r \rightarrow \text{OK}$$

Shear @ Bottom:

$$V := V + F_{wind}$$

$$V = 375 \cdot \text{lb} \cdot \text{ft} < V_r \rightarrow \text{OK}$$

REQUIRED SECTION: 18" x 131

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## SECTION 3

Tower Section Length:

$$L_s := 8 \cdot \text{ft}$$

Section Size Index:

$$i := 2$$

Leg Tube Index:

$$j := 2$$

Wind Area:

$$A_{w_{i,j}} = 3 \text{ ft}^2$$

Allowable Moment:

$$M_{R_{i,j}} = 22100 \cdot \text{lb} \cdot \text{ft}$$

Weight:

$$W_{s_{i,j}} = 40 \cdot \text{lb} \cdot \text{ft}$$

Allowable Shear:

$$V_{R_{i,j}} = 1230 \cdot \text{lb} \cdot \text{ft}$$

Bottom Height:

$$h := h - L_s$$

$$h = 45 \text{ ft}$$

Wind Force on Section:

$$F_{wind} := P_w \left( h + \frac{L_s}{2}, bws \right) \cdot A_{w_{i,j}}$$

$$F_{wind} = 39.6 \cdot \text{lb} \cdot \text{ft}$$

Weight @ Bottom:

$$W := W + W_{s_{i,j}}$$

$$W = 281 \cdot \text{lb} \cdot \text{ft}$$

Moment @ Bottom:

$$M := M + V \cdot L_s + F_{wind} \cdot \frac{L_s}{2} + \frac{W}{3} \cdot d_i$$

$$M = 8911 \cdot \text{lb} \cdot \text{ft} < M_r \rightarrow \text{OK}$$

Shear @ Bottom:

$$V := V + F_{wind}$$

$$V = 415 \cdot \text{lb} \cdot \text{ft} < V_r \rightarrow \text{OK}$$

REQUIRED SECTION: 18" x 172

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## SECTION 4

Tower Section Length:	$L_{s,v} := 8 \cdot \text{ft}$		
Section Size Index:	$i := 3$	Leg Tube Index:	$j_v := 2$
Wind Area:	$A_{w,i,j} = 3.3 \text{ ft}^2$	Allowable Moment:	$M_{R,i,j} = 26900 \cdot \text{lbf} \cdot \text{ft}$
Weight:	$W_{s,i,j} = 46 \cdot \text{lbf}$	Allowable Shear:	$V_{R,i,j} = 1820 \cdot \text{lbf}$
Bottom Height:	$h := h - L_s$		$h = 37 \text{ ft}$
Wind Force on Section:	$F_{wind} := P_w \left( h + \frac{L_s}{2}, bws \right) \cdot A_{w,i,j}$		$F_{wind} = 42.1 \cdot \text{lbf}$
Weight @ Bottom:	$W := W + W_{s,i,j}$		$W = 327 \cdot \text{lbf}$
Moment @ Bottom:	$M := M + V \cdot L_s + F_{wind} \cdot \frac{L_s}{2} + \frac{W}{3} \cdot d_i$		$M = 12558 \cdot \text{lbf} \cdot \text{ft} < M_r \rightarrow \text{OK}$
Shear @ Bottom:	$V := V + F_{wind}$		$V = 457 \cdot \text{lbf} < V_r \rightarrow \text{OK}$

REQUIRED SECTION: 22" x 172

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## SECTION 5

Tower Section Length:	$L_{s,v} := 8 \cdot \text{ft}$		
Section Size Index:	$i := 3$	Leg Tube Index:	$j_v := 3$
Wind Area:	$A_{w,i,j} = 4 \text{ ft}^2$	Allowable Moment:	$M_{R,i,j} = 47200 \cdot \text{lbf} \cdot \text{ft}$
Weight:	$W_{s,i,j} = 65 \cdot \text{lbf}$	Allowable Shear:	$V_{R,i,j} = 1820 \cdot \text{lbf}$
Bottom Height:	$h := h - L_s$		$h = 29 \text{ ft}$
Wind Force on Section:	$F_{wind} := P_w \left( h + \frac{L_s}{2}, bws \right) \cdot A_{w,i,j}$		$F_{wind} = 49.1 \cdot \text{lbf}$
Weight @ Bottom:	$W := W + W_{s,i,j}$		$W = 392 \cdot \text{lbf}$
Moment @ Bottom:	$M := M + V \cdot L_s + F_{wind} \cdot \frac{L_s}{2} + \frac{W}{3} \cdot d_i$		$M = 16601 \cdot \text{lbf} \cdot \text{ft} < M_r \rightarrow \text{OK}$
Shear @ Bottom:	$V := V + F_{wind}$		$V = 506 \cdot \text{lbf} < V_r \rightarrow \text{OK}$

REQUIRED SECTION: 22" x 225

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**SECTION 6**

Tower Section Length:	$L_s := 8 \cdot \text{ft}$	Leg Tube Index:	$j := 3$
Section Size Index:	$i := 4$	Allowable Moment:	$M_{R,i,j} = 56400 \cdot \text{lb} \cdot \text{ft}$
Wind Area:	$A_{w,i,j} = 4.2 \cdot \text{ft}^2$	Allowable Shear:	$V_{R,i,j} = 2350 \cdot \text{lb} \cdot \text{ft}$
Weight:	$W_{s,i,j} = 73 \cdot \text{lb} \cdot \text{ft}$		
Bottom Height:	$h := h - L_s$		$h = 21 \text{ ft}$
Wind Force on Section:	$F_{wind} := P_w \left( h + \frac{L_s}{2}, bws \right) \cdot A_{w,i,j}$		$F_{wind} = 49.0 \cdot \text{lb} \cdot \text{ft}$
Weight @ Bottom:	$W := W + W_{s,i,j}$		$W = 465 \cdot \text{lb} \cdot \text{ft}$
Moment @ Bottom:	$M := M + V \cdot L_s + F_{wind} \cdot \frac{L_s}{2} + \frac{W}{3} \cdot d_i$		$M = 21118 \cdot \text{lb} \cdot \text{ft} < M_r \rightarrow \text{OK}$
Shear @ Bottom:	$V := V + F_{wind}$		$V = 555 \cdot \text{lb} \cdot \text{ft} < V_r \rightarrow \text{OK}$

**REQUIRED SECTION: 26" x 225**

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**SECTION 7**

Tower Section Length:	$L_s := 8 \cdot \text{ft}$	Leg Tube Index:	$j := 3$
Section Size Index:	$i := 5$	Allowable Moment:	$M_{R,i,j} = 65600 \cdot \text{lb} \cdot \text{ft}$
Wind Area:	$A_{w,i,j} = 4.4 \cdot \text{ft}^2$	Allowable Shear:	$V_{R,i,j} = 1990 \cdot \text{lb} \cdot \text{ft}$
Weight:	$W_{s,i,j} = 77 \cdot \text{lb} \cdot \text{ft}$		
Bottom Height:	$h := h - L_s$		$h = 13 \text{ ft}$
Wind Force on Section:	$F_{wind} := P_w \left( h + \frac{L_s}{2}, bws \right) \cdot A_{w,i,j}$		$F_{wind} = 48.2 \cdot \text{lb} \cdot \text{ft}$
Weight @ Bottom:	$W := W + W_{s,i,j}$		$W = 542 \cdot \text{lb} \cdot \text{ft}$
Moment @ Bottom:	$M := M + V \cdot L_s + F_{wind} \cdot \frac{L_s}{2} + \frac{W}{3} \cdot d_i$		$M = 26122 \cdot \text{lb} \cdot \text{ft} < M_r \rightarrow \text{OK}$
Shear @ Bottom:	$V := V + F_{wind}$		$V = 603 \cdot \text{lb} \cdot \text{ft} < V_r \rightarrow \text{OK}$

**REQUIRED SECTION: 30" x 225**

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**BASE SECTION**

Tower Section Length:	$L_{ws,j} := 8 \cdot \text{ft}$	Leg Tube Index:	$j := 4$
Section Size Index:	$i := 5$	Allowable Moment:	$M_{R,i,j} = 96300 \cdot \text{lb} \cdot \text{ft}$
Wind Area:	$A_{w,i,j} = 5.2 \text{ft}^2$	Allowable Shear:	$V_{R,i,j} = 2050 \cdot \text{lb}$
Weight:	$W_{s,i,j} = 96 \cdot \text{lb}$	Bottom Height:	$h := h - L_s$ $h = 5 \text{ft}$
Wind Force on Section:	$F_{wind} := P_w \left( h + \frac{L_s}{2}, bws \right) \cdot A_{w,i,j}$		$F_{wind} = 55.8 \cdot \text{lb}$
Weight @ Bottom:	$W_{ww} := W + W_{s,i,j}$		$W = 638 \cdot \text{lb}$
Moment @ Bottom:	$M_{ww} := M + V \cdot L_s + F_{wind} \cdot \frac{L_s}{2} + \frac{W}{3} \cdot d_i$		$M = 31607 \cdot \text{lb} \cdot \text{ft} < M_r \rightarrow \text{OK}$
Shear @ Bottom:	$V_{ww} := V + F_{wind}$		$V = 659 \cdot \text{lb} < V_r \rightarrow \text{OK}$

**REQUIRED SECTION: 30" x 288**

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## FOOTING DESIGN -- 64' Tower 22 sq. ft. in winds of 80 mph

Materials:	Concrete:	$f_c := 2500 \cdot \text{psi}$	For design, min. 3000 psi to be specified.
	Reinforcement:	$f_y := 60 \cdot \text{ksi}$	
	Threaded Anchor Rod Legs, B-7 alloy:	$f_z := 144 \cdot \text{ksi}$	

### FOOTING SIZE BASED ON SOIL REQUIREMENTS (IBC 2009 Sec. 1806.7.3)

Applied Moment:  $M = 31.6 \cdot \text{k} \cdot \text{ft}$

Applied Horizontal Force:  $V = 0.66 \cdot \text{k}$

Base Section Size:  $b_{ss} := 30 \cdot \text{in}$

Effective Height of Horizontal Force:  $h' := \frac{M}{V} \quad h' = 48.0 \text{ ft}$

Soil Bearing Pressure:  $S_1 := 150 \text{ pcf}$

IBC 2009 Table 1806.2. Based on sand, silty sand, clayey sand, silty gravel and clayey gravel

$$b := \frac{b_{ss} + 2.88 \cdot \text{in}}{\sin(60 \cdot \text{deg})} + 7 \cdot \text{in} \quad b = 45.0 \cdot \text{in} \quad \text{USE: } b_{\text{MIN}} := 60 \cdot \text{in}$$

Depth of Embedment:  
IBC 2009 Sect  
1807.3.2 Eq 18-1

$$D_{\text{reqd}} := \text{root} \left[ D - 0.5 \left[ \frac{2.34 \cdot V}{\left(\frac{D}{3}\right) \cdot S_1 \cdot b} \right] \cdot \left[ 1 + \sqrt{1 + \frac{4.36 \cdot h'}{\left(\frac{D}{3}\right) \cdot S_1 \cdot b}} \right] \right], D$$

$$D_{\text{reqd}} = 7.16 \cdot \text{ft}$$

### CONCRETE FOOTING DESIGN (IBC 2009 Sec. 1810)

**Note:** Vertical load is negligible compared to moment, so design as flexure without axial load; use singly-reinforced approach to be conservative.

Design Moment  $M_f := \frac{[M + V \cdot (2 \cdot b)]}{0.6} \quad M_f = 63.7 \cdot \text{k} \cdot \text{ft}$

Factored Moment:  $M_u := 1.0 \cdot M_f \quad M_u = 63.7 \cdot \text{k} \cdot \text{ft}$

Reduction Factor:  $\phi := 0.9$

Over-Reinforcement:  $\text{ORF} := 1.33$

Effective Depth:  $d_{\text{MIN}} := \frac{b}{2} + \left(\frac{b}{2} - 4 \cdot \text{in}\right) \cdot \sin(60 \cdot \text{deg}) \quad d = 52.517 \cdot \text{in}$

Angle of Circular Segment Compression Block:

$$\Theta(r, A_s) := \text{root} \left[ \frac{A_s \cdot f_y}{0.85 \cdot f_c} - \left[ \pi \cdot r^2 \cdot \left(\frac{\theta}{2 \cdot \pi}\right) - \frac{2 \cdot r \cdot \sin\left(\frac{\theta}{2}\right) \cdot \left(r - \frac{2 \cdot r \cdot \sin\left(\frac{\theta}{2}\right)}{2} \cdot \tan\left(\frac{\theta}{4}\right)\right)}{2} \right] \right], \theta$$

5' x 5' or 5' DIA ROUND HOLE, 7.16' DEEP

Distance from Extreme  
Fiber to Centroid of  
Compression Block:

$$y(\alpha) := \frac{b}{2} - \frac{b}{3} \cdot \left( \frac{\sin(\alpha)^3}{\alpha - \sin(\alpha) \cdot \cos(\alpha)} \right)$$

Required Tension  
Steel:

$$A_s := \text{root} \left[ \phi \cdot A_s \cdot f_y \cdot \left( d - y \left( \frac{\Theta \left( \frac{b}{2}, A_s \right)}{2} \right) \right) - M_u, A_s \right] \cdot \text{ORF} \quad A_s = 0.36 \cdot \text{in}^2$$

Try #6 Bars, on each side:

$$A_b := .44 \cdot \text{in}^2 \quad A_{ss} := 2 \cdot A_b \quad A_s = 0.88 \cdot \text{in}^2$$

Check Factored  
Nominal Moment:

$$\phi M_n := \phi \cdot A_s \cdot f_y \cdot \left( d - y \left( \frac{\Theta \left( \frac{b}{2}, A_s \right)}{2} \right) \right) \quad \phi M_n = 203.7 \cdot \text{k} \cdot \text{ft} > M_u \therefore \text{OK}$$

**REQUIRED FOOTING: 5'-0" x 7' 2" DEEP FOOTING W/ (6) #6 VERTICAL BARS W/ STANDARD HOOKS @ TOP & (6) #3 CIRCULAR TIES @ 4" AT TOP, #3 CIRCULAR TIES @ 12" ELSEWHERE.**

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**NOTICE**

*To the best of our knowledge, the information presented herein is accurate and in compliance with the 2009 International Building Code. However, this information is intended only to demonstrate structural calculation methodology; actual tower system calculations must be performed by a registered structural engineer. Neither Heights Tower Systems, the authors, nor any of their affiliates assumes any liability for any errors, omissions, negligence or any other deficiencies that may result from the use of the information contained herein. The responsibility for determination of suitability of the information, selection of proper product, installation, placement, and adequacy of supporting structures lies solely with the purchaser.*